

The mathematical approach for HIV infection is studied under 3 different models:

- 1) Uninfected Model
- 2) Infected Model
- 3) Mutations Model

#### UNINFECTED MODEL:

The equation for the uninfected model involves four components:

Normal Tcells, Latently infected T cells, Actively infected T cells and the Virus itself.

$$\frac{dT}{dt} = s + rT\left(1 - \frac{T}{T_{\max}}\right) - \mu T$$

- T - T cell Population in cells
- $T_{\max}$  - Maximum T cell Population
- s - T cell from precursor supply rate
- r - Normal T cell growth rate
- $\mu$  - T cell Death Rate

The Steady State solution for the equation is obtained by making the derivative  $dT/dt$  equal to 0.

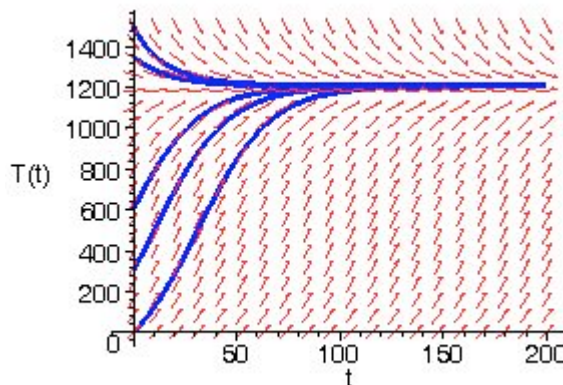
We obtain :

$$T_0 = \frac{T_{\max}}{2r} \left( p + \sqrt{p^2 + 4s \frac{r}{T_{\max}}} \right)$$

Where  $p = r - \mu$

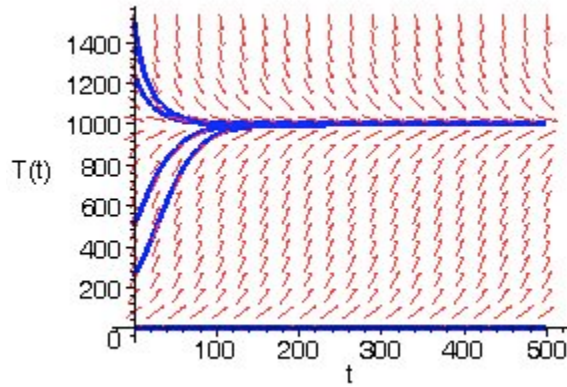
Steady States for Different parameters when  $s = 10$ ,  $r = 0.06$ ,  $T_{\max} = 1500$ ,  $\mu = 0.02$

Situation:1



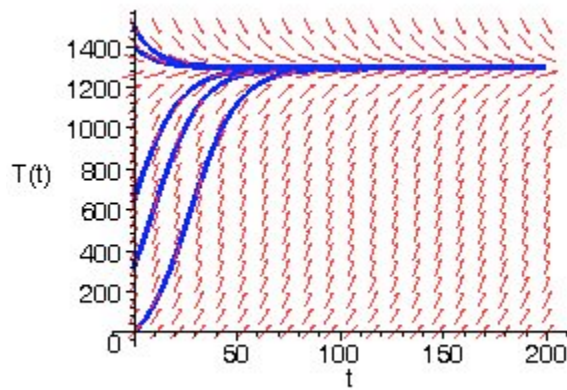
We Obtain  $T_0 = 1207.1$

Situation 2: Steady States when  $s = 0$ ,  $r = 0.06$ ,  $T_{\max} = 1500$ ,  $\mu = 0.02$



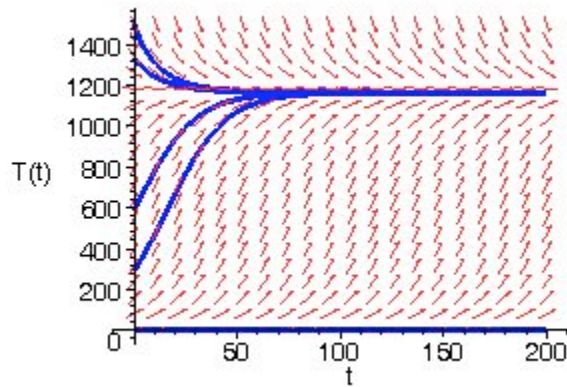
We Obtain  $T_0 = 1000$

Situation 3: The Steady States when  $s = 10$ ,  $r = 0.09$ ,  $T_{\max} = 1500$ ,  $\mu = 0.02$



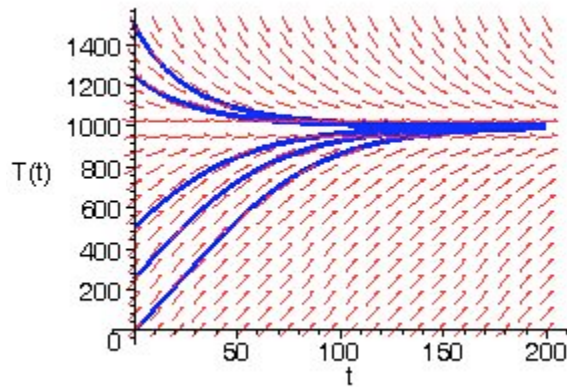
We Obtain  $T_0 = 1295.33$

Situation 4: The Steady States when  $s = 0$ ,  $r = 0.09$ ,  $T_{\max} = 1500$ ,  $\mu = 0.02$



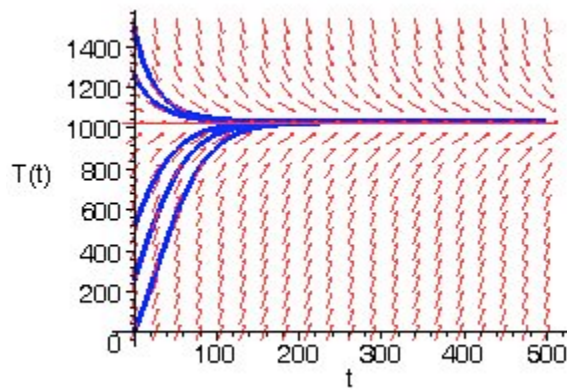
We Obtain  $T_0 = 1166.66$

Situation 5: The Steady States when  $s = 10$ ,  $r = 0.03$ ,  $T_{\max} = 1500$ ,  $\mu = 0.02$



We Obtain  $T_0 = 1000$

Situation 6: The Steady States when  $r$  is increased by 10% .  
Hence  $s = 10$ ,  $r = 1.1 \cdot 0.03$ ,  $T_{\max} = 1500$ ,  $\mu = 0.02$ .



We Obtain  $T_0 = 1031.55$

INFECTED MODEL:

There four system of equations used to Model T-cell HIV interaction.